

## 3.4 Velocity and Other Rates of Change

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### Instantaneous Rate of Change

$$f'(a) = \lim_{h \rightarrow 0} \frac{f(a+h) - f(a)}{h}$$

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### Velocity, Speed, and Acceleration

If the position function is described by  $s(t)$ , then

$$\text{velocity} = v(t) = s'(t)$$

$$\text{speed} = |v(t)| = |s'(t)|$$

$$\text{acceleration} = a(t) = v'(t) = s''(t)$$

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### Free – fall Constants on Earth

$$\text{English units} \quad \rightarrow \quad s = -16t^2 \quad a = -32 \frac{\text{ft}}{\text{sec}^2}$$

$$\text{Metric units} \quad \rightarrow \quad s = -4.9t^2 \quad a = -9.8 \frac{\text{m}}{\text{sec}^2}$$

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### Marginal Cost

Marginal Cost is the derivative of the Cost function.

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1. A particle moves along a line so that its position at any time  $t \geq 0$  is given by  $s(t) = t^2 - t - 4$ , where  $s$  is measured in meters and  $t$  is measured in seconds. Find

- the displacement in the first 3 seconds
  - the average velocity in the first 3 seconds
  - the acceleration at  $t = 3$  seconds
  - where the particle is when  $s$  is a minimum
  - the velocity when  $t = 3$  seconds
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2. A calculus book thrown vertically upward on the planet Zorgon at a velocity of  $27 \frac{\text{m}}{\text{sec}}$

reaches a height of  $s = 27t - 0.6t^2$  meters in  $t$  seconds

- Find the book's velocity and acceleration as functions of time
- Find how long does it take the book to reach its highest point
- Find how high the book goes
- Find how long the book is aloft

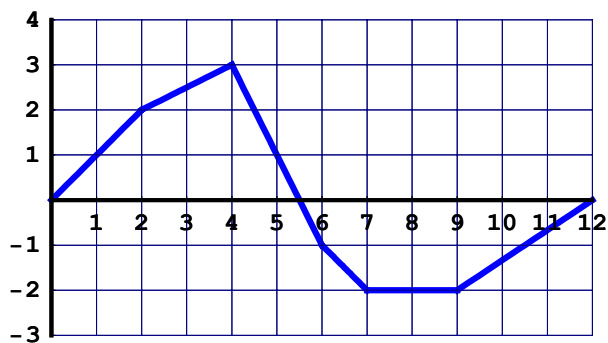
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3. Suppose it costs  $c(x) = x^3 - 3x^2 + 8x + 4$  dollars to produce  $x$  widgets when 5 to 15 widgets are produced. Find the marginal cost for 7 widgets.

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4. The following graph relates time and velocity for a particle moving along a coordinate line

- (a) find when the particle reverses direction
- (b) find when the body is moving at a constant speed
- (c) graph the particle's speed
- (d) graph the particle's acceleration



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5. 

t(seconds)	0	3	6	9	12	15	18	21
s(feet)	0	8	12	15	16	14	21	13

Given the table above, relating time and position, approximate the velocity and acceleration at time  $t = 9$  seconds